



Empirical investigation of starling flocks: a benchmark study in collective animal behaviour

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Bird flocking is a striking example of collective animal behaviour. A vivid illustration of this phenomenon is provided by the aerial display of vast flocks of starlings gathering at dusk over the roost and swirling with extraordinary spatial coherence. Both the evolutionary justification and the mechanistic laws of flocking are poorly understood, arguably because of a lack of data on large flocks. Here, we report a quantitative study of aerial display. We measured the individual three-dimensional positions in compact flocks of up to 2700 birds. We investigated the main features of the flock as a whole (shape, movement, density and structure) and we discuss these as emergent attributes of the grouping phenomenon. Flocks were relatively thin, of various sizes, but constant proportions. They tended to slide parallel to the ground and, during turns, their orientation changed with respect to the direction of motion. Individual birds kept a minimum distance from each other that was comparable to their wing span. The density within the aggregations was nonhomogeneous, as birds were packed more tightly at the border than the centre of the flock. These results constitute the first set of large-scale data on three-dimensional animal aggregations. Current models and theories of collective animal behaviour can now be tested against these data.

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The aerial display of large flocks of birds is a stunning example of collective behaviour in animal aggregations (Emlen 1952). A paradigmatic case is provided by European starlings, *Sturnus vulgaris* (Feele 1984). These birds can be observed in many cities, where they establish their roosting

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sites. Shortly before sunset, starlings return to their roost and, prior to retiring for the night, they form sharp-bordered flocks, ranging from a few hundred to tens of thousands of birds, which wheel and turn over the roosting site until darkness falls. Flocks show strong spatial coherence and are capable of fast, highly synchronized manoeuvres, either spontaneously, or as a response to predator attacks. Many features of bird flocking are present in other instances of collective animal behaviour. Fish schools, mammal herds and insect swarms represent other examples of animal aggregations that have fascinated biologists for many years (Gueron et al. 1996; Parrish & Edelstein-Keshet 1999; Krause & Ruxton 2002; Couzin & Krause 2003). Like starlings, individuals of these other taxa form cohesive groups that are able to sustain remarkable coordination and adaptability.

Diverse instances of collective behaviour are found in many different fields of science, from the spontaneous ordering of magnetic moments in physics (e.g. Cardy 1996), the coordination of an ensemble of artificial agents with distributed intelligence in robotics (Cao et al. 1997; Jadabaie et al. 2003), the emergence of herding behaviour in financial markets in economics (Cont & Bouchaud 2000), to the synchronized clapping in a concert hall (Neda et al. 2000; Michard & Bouchaud 2005) or the Mexican wave in a stadium (Farkas et al. 2002). In all these examples, collective behaviour emerges as the result of the local interactions between the individual units, without the need for centralized coordination. The tendency of each agent to imitate its neighbours (allelomimesis), can, by itself, produce a global collective state. Whenever this happens, we are in the presence of self-organized collective behaviour.

Although self-organization is undoubtedly a general and robust mechanism, its universality is an open issue. In physics, for example, universality is a well-defined concept: the same model and theory can be used to describe quantitatively very different physical systems, provided that they all share the same fundamental symmetries. The situation is more complicated in biology because the individuals that form a group are much more complex than particles or spins. For example, although fish schools and bird flocks behave similarly, certain collective patterns are present in one case and not in the other (Krause & Ruxton 2002). At some level, the specificities of the individuals and of the environment must make a difference. Therefore, in view of the highly interdisciplinary nature of self-organized collective behaviour, it is important to distinguish the general from the specific.

Models play a crucial role in this respect. Indeed, it was modelling exercises that revealed the general principles of how collective behaviour can emerge from self-organization. When it comes to modelling real instances of collective behaviour, however, we need to be more detailed. In this case, models must specify the minimal rules necessary to reproduce the empirical observations, so that we can distinguish between general phenomena and those specific to the system.

The field of collective animal behaviour boasts a wealth of models (Aoki 1982; Reynolds 1987; Heppner & Grenader 1990; Huth & Wissel 1992; Vicsek et al. 1995; Couzin et al. 2002; Inada & Kawachi 2002; Kunz & Hemelrijk 2003; Gregoire & Chaté 2004). Some of these were developed for fish schools, some for bird flocks, and some with a nonspecific biological target. In all cases, however, the models agree on three general behavioural rules: move in the same direction as your neighbours; remain close to them; avoid collisions. These rules are modelled using three distinct contributions to the interactions among the individuals, that is, alignment of velocities, attraction and short-range repulsion. In all cases, the models produce cohesive aggregations that look qualitatively similar to natural cases. However, each model has its own way of implementing the rules, dictated by the differing opinions as to which are the relevant mechanisms and by the different biological targets (e.g. fish versus birds). Of course, selection among different models can be achieved only by comparing their results with empirical evidence. Only empirical

observations can tell us whether or not the collective properties of a model are in quantitative agreement with the natural case. Moreover, the feedback between models and empirical data must confirm whether or not a certain rule is truly necessary to reproduce a specific biological feature.

Empirical data, then, are necessary both as a crucial input of the modelling approach and as a quantitative guideline for answering more fundamental questions about groups, their global features and biological function (see e.g. Parrish & Hammer 1997). Unfortunately, 3D data on even moderately large groups of animals are hard to obtain, and quantitative empirical data are scarce and limited to small groups (a few tens of individuals). Testing of the models has therefore been sporadic so far. At the same time, speculation on the microscopic origin and biological function of collective behaviour has outgrown empirical groundwork.

Empirical 3D studies on fishes have been done in laboratory tanks (Cullen et al. 1965; Partridge 1980; Partridge et al. 1980; Van Long et al. 1985; Tien et al. 2004). Data for birds, on the other hand, have been obtained in field observations (Miller & Stephen 1966; van Tets 1966; Major & Dill 1978; Pomeroy & Heppner 1992; Budgey 1998). These studies, however, have two major limitations: the number of individuals is small (limited to a few tens of individuals) and the group arrangements are loose, at variance with the huge, highly cohesive groups characteristic of collective behaviour. Both these drawbacks stem from a single technical problem: to reconstruct the 3D position of an object, all optical techniques (stereometry, orthogonal method, shadow method) require different images to be placed in correspondence (i.e. to be matched, Fig. 1a, b; Osborn 1997; Hartley & Zisserman 2003). For large and compact sets of featureless points, this problem is so severe that it has been suggested that these techniques are fundamentally inadequate to handle 3D biological aggregations (Aloimonos & Rosenfeld 1991).

Using statistical physics, optimization theory and computer vision techniques, we have managed to solve the correspondence problem. We developed an experimental technique capable of reconstructing the individual 3D positions in cohesive aggregations of several thousands of animals in the field (Cavagna et al. 2008a). We used this technique to collect quantitative empirical data on large flocks of starlings during aerial display. In this paper, we present quantitative and systematic data on the two main attributes of the groups: global properties (shape, size, orientation and movement) and internal structure (density profile and distribution of neighbours). Our aim in doing so is two-fold.

(1) We wish to provide a detailed analysis of the mechanistic laws of flocking, at the global and structural levels. This enables us to set a new experimental benchmark for testing existing models of self-organized collective behaviour.

(2) We wish to characterize the attributes of flocks as emergent properties of the grouping phenomenon. To this end, we attempt to place our results in the context of the biological function of grouping, individual fitness consequences, interaction with the environment and mutual interaction between individuals.

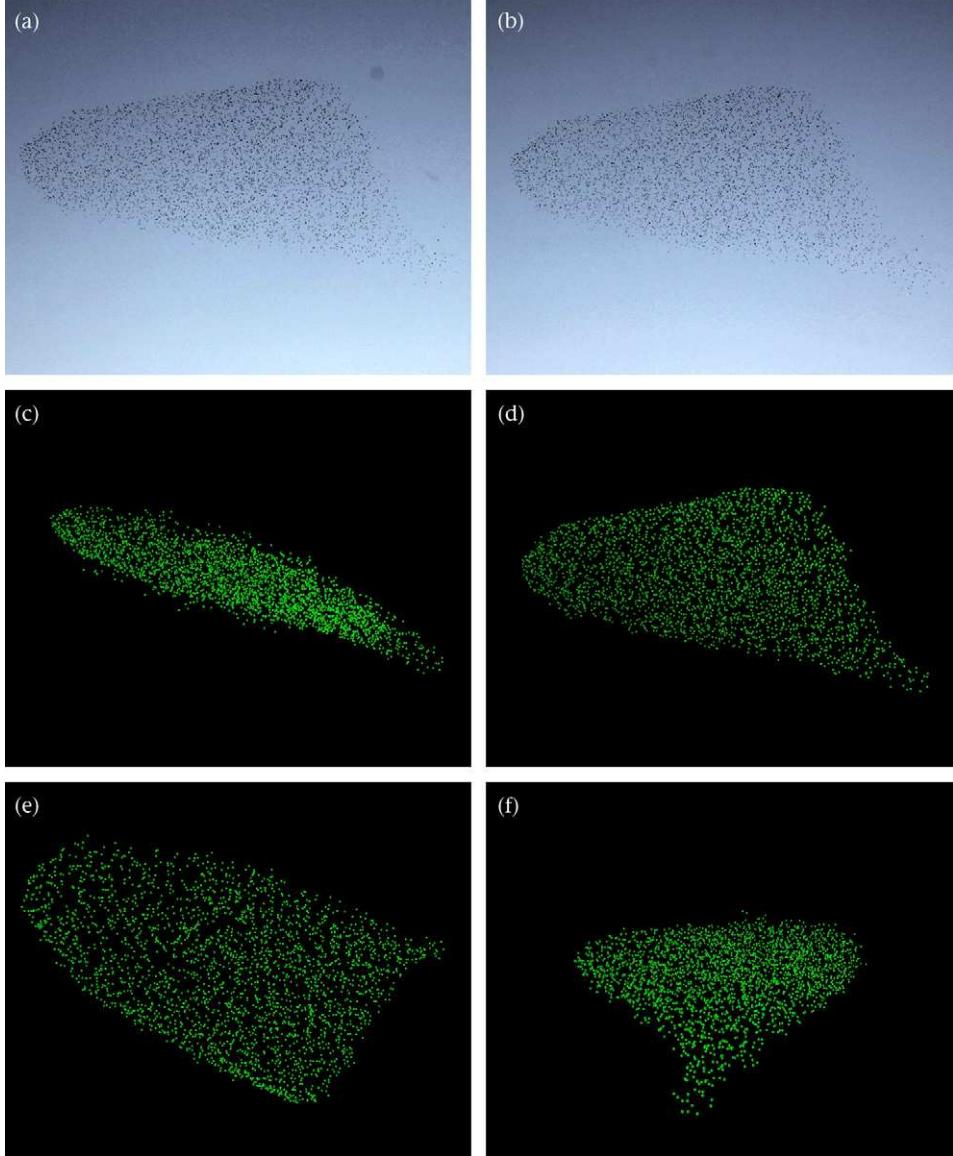


Figure 1. A typical flock and its 3D reconstruction. This flock (16-05) consists of 2630 starlings, flying at approximately 240 m from the cameras. The cameras' tilt-up was 40%. (a, b) Left-hand and right-hand, photos of the stereo pair, taken at the same time, but 25 m apart. For the 3D reconstruction, each bird's image on the left-hand photo must be matched to its corresponding image on the right-hand photo. (c–f) 3D reconstruction of the flock in the reference frame of the right-hand camera, under four different points of view. (d) Shows the reconstructed flock with the same perspective as (b).

METHODS

Both the experimental technique used to obtain 3D data and the statistical tools used to analyse the data are reported in detail elsewhere (Cavagna et al. 2008a, b). In the present section, therefore, we give only a brief summary of the most essential points.

Location and Materials

Large colonies of European starlings spend the winter in Rome, Italy, where several roosting sites are located within the city urban area. In our analysis we did not consider migrating flocks, or travelling flocks, that is, flocks that

move from feeding to roosting site. Instead, we focused only on those engaged in aerial display: shortly before dusk, cohesive flocks of starlings swirl over the roost, wandering in a wide but confined area. We took digital images of starling aerial display at the roosting site of Termini railway station, between December 2005 and February 2006, from the terrace of Palazzo Massimo, Museo Nazionale Romano. The apparatus was located 30 m above ground level. Wind speed never exceeded 12 m/s. On average, birds were 100 m from the cameras. We used Canon EOS 1D Mark II digital cameras (3504×2336 pixels), mounting Canon 35 mm lenses. The aperture was set between f2.0 and f4.0, shutter speed between 1/1000 and 1/250 s, ISO between 100 and 800, and cameras' tilt-up between 35 and 40%.

Experimental Technique

We used stereophotography to collect data on flocks (Longuet-Higgins 1981; Osborn 1997). More specifically, we used the trifocal technique (Hartley & Zisserman 2003), with three different points of view. The distance between the two stereocameras (the baseline) was $d = 25$ m. Given two targets at 100 m from the apparatus, with a relative distance of 1 m, our tests gave an error of $\delta z < 0.04$ m on the relative distance, and an error of $\Delta z < 0.92$ m on the absolute distance of the targets. The error is thus below 5% for both the relative and absolute distance. Our apparatus shot series of photographs at a rate of 10 frames/s for a maximum of 8 s (80 consecutive photographs). After that, the cameras' buffer filled up and we had to wait a few seconds before another series of photographs could be taken. If the flock under consideration left the field of view of any of the cameras, the series was interrupted. The algorithms used to solve the correspondence problem and do the 3D reconstruction are described in Cavagna et al. (2008a). In the cases we analysed, we reconstructed on average 88% of the birds, and never less than 80% of the flock.

Events Selection

A flocking event was defined as a series of up to 80 consecutive photographs shot at 10 frames/s of a single flock. We collected on average 15 events every session, and we thus gathered approximately 500 flocking events over 40 sessions. Not all of these events, however, could be processed. The vast majority of them were not in the common field of view of all the cameras, a necessary condition for the 3D reconstruction. In addition, the flock had to be within 250 m of the cameras (because of our photographic resolution); the total number of objects in the photograph had to be fewer than 8000 birds (because of software constraints); and exposure and contrast had to be appropriate. Only 50 events met these criteria. We then selected 20 of these, choosing flocks with sharp borders, strong spatial cohesion and a large number of birds ($N > 400$). Finally, our matching algorithm put a limit to the flock's maximum density on the photographs, leaving only 10 events suitable for analysis. Using synthetic data, we checked that the reconstruction software did not introduce any significant bias in the flocks' shape and structure.

Biological Target of Investigation

Qualitatively, we could distinguish between two classes of aerial display. Some flocks flew very high above the roost (>200 m): they were typically very large (tens of thousands of birds) with a columnar-like shape and performed the most striking changes in formation patterns. These flocks were visible from very far away, owing to their size, altitude and change in density. Fear (1984) suggested that such flocks may act as a beacon to signal the location of the roost to conspecifics. These groups were too far away to allow us to use our reconstruction procedure effectively, as optical resolution is the main bottleneck. Moreover, the pattern of these flocks seems to be specific to starlings, whereas we were interested in more general features of collective

behaviour. Therefore we do not address these kinds of flock here. The other kind of flock flew at a lower altitude (<100 m), right over the roost. They were usually smaller, ranging from a few hundred to several thousand birds and were usually compact, with sharp-bordered edges. These flocks performed a random walk above the roost, keeping the same global features for quite long timescales. In other words, they showed a form of steady-state behaviour, which makes them a good target for statistical investigation. These flocks are the ones we were able to reconstruct accurately and the present study therefore focuses on the properties of these flocks.

Methods of Analysis

The reconstruction provided us with the 3D coordinates of each individual bird in the flock. The next step was to identify the border of the flock. Standard tools, such as the convex hull, are inadequate given the presence of concavities at different scales. Rather, we used the α -shape algorithm (Edelsbrunner & Mücke 1994), a method that allows the pinpointing of concavities of the boundary down to a given scale α . This algorithm identifies a nonconvex border that appropriately follows the external concavities and faithfully reproduces the external shape. This procedure allowed us to identify birds that belonged to the border and all the others were therefore identified as 'internal' birds. Typically, birds on the border, or close to it, have statistical properties that are different from internal birds. When computing structural features (such as neighbour distribution, average distances and so on) one needs to take into account these boundary effects to produce unbiased data. In all our analysis, we used appropriate techniques to deal with this problem, as explained in Cavagna et al. (2008b).

Once the border was defined, the volume of the flock was computed via the Delaunay triangulation, identifying the subensemble of the triangulation internal to the border. Flocks typically had asymmetric shapes, thinner in one direction and more extended along the other two. To characterize this shape in a quantitative way, we defined the three main dimensions and axes of the flock (Cavagna et al. 2008b). The shortest dimension, the thickness I_1 , was defined as the diameter of the largest sphere contained within the flock's boundary. We then fitted a plane to the flock and defined the axis orthogonal to this plane as the yaw axis relative to I_1 . We refer to this axis by means of a unit vector \mathbf{I}_1 parallel to it. Since the flock extends in space mostly orthogonally to \mathbf{I}_1 , we could exploit the fitted plane to identify the two largest dimensions. The flock was then projected onto this plane. Following a similar strategy as before, we defined the second dimension I_2 as the diameter of the smallest circle contained in the flock's projection on the plane. We then fitted the 2D projection of the flock to a line, which identified the axis \mathbf{I}_3 along the flock and the corresponding largest dimension I_3 . The orthogonal direction to \mathbf{I}_3 on the plane defined the axis \mathbf{I}_2 relative to the intermediate dimension I_2 . The three unitary axes \mathbf{I}_1 , \mathbf{I}_2 and \mathbf{I}_3 are by construction orthogonal to each other and can be used to describe the orientation of the flock in space. For example, the main axis \mathbf{I}_3 represents the direction along

which the flock is more extended: by measuring the mutual orientation of \mathbf{I}_3 with the velocity we can identify whether or not the flock is elongated along the direction of motion.

The three dimensions I_1 , I_2 and I_3 give a quantitative description of the flock's shape. For example, if I_1 , I_2 and I_3 assumed values comparable to each other this means that the flock has an approximately symmetrical shape (in the case of a sphere or of a cube, one finds $I_1 = I_2 = I_3$). If I_1 is much smaller than I_2 and I_3 then the group is very thin along the smallest axes and extends more perpendicularly to it. From these examples it is clear that what matters are the relative and not the absolute values of these dimensions. For this reason we considered ratios between the dimensions in our analysis (see [Results](#)).

RESULTS

Morphology

[Figure 1](#) shows a typical example of a flock, together with its 3D reconstruction. By rotating the point of view, one can immediately see the striking thinness of the flock ([Fig. 1c](#)). To characterize the shape and thinness of the flock, we considered its three dimensions $I_1 < I_2 < I_3$ and measured the aspect ratios, that is, the ratios of the two longer dimensions to the shortest one: I_2/I_1 and I_3/I_1 ([Table 1](#)). Despite some fluctuations across flocks, these ratios were generally stable, and showed no significant dependence on the number of birds or the volume of the flocks ([Fig. 2b](#)). The average over all events gives: $I_2/I_1 = 2.8 \pm 0.4$ and $I_3/I_1 = 5.6 \pm 1.0$ (confidence intervals of 95% throughout the paper), confirming the visual impression that flocks were generally thin.

In contrast, the flock's thickness I_1 , that is, the shortest dimension, was highly variable. We can explain this by noting that if the aspect ratios I_2/I_1 and I_3/I_1 are constant,

the thickness I_1 must be linearly correlated with $V^{1/3}$, where V is the flock's volume. This is accurately verified by our data ([Fig. 2a](#)). Therefore, whereas the number of individuals and the flock's volume changed significantly from flock to flock, the flock's proportions remained approximately constant.

The concavity of a flock can be quantified as the relative difference between the volume of the convex hull (smallest convex polyhedron enclosing the flock) and the volume of the aggregation computed with the α -shape method ([Table 1](#)). Some flocks showed a nonzero concavity, which indicates that defining their border with the convex hull would be inappropriate, since this method would include large portions of space devoid of animals. Unlike the aspect ratio, however, there was no typical value for the concavity.

Orientation

Given the highly nonspherical shape of flocks, we can ask whether or not they have a preferential orientation in space. To investigate this, we looked at the flock axes \mathbf{I}_1 , \mathbf{I}_2 , and \mathbf{I}_3 . We defined the unit vector \mathbf{G} as parallel to gravity and computed the inner product of \mathbf{I}_1 and \mathbf{G} , that is, the cosine between yaw and gravity. This quantity was close to 1 in most flocks ([Table 1](#), [Fig. 3](#)) and, on average, $|\mathbf{I}_1 \cdot \mathbf{G}| = 0.93 \pm 0.04$. This shows that the yaw axis was approximately parallel to gravity, and therefore that the flock's plane was parallel to the ground. The relation between orientation in space and global movement of the flock is also of interest. We defined the centre of mass as the average position of all birds in the flock, and then measured its direction of motion. Such a direction is identified by a unit vector \mathbf{V} , representing the normalized velocity. The orientation of flight can be described by the scalar product of the unitary velocity \mathbf{V} with gravity and yaw ([Table 1](#)). Both these quantities were small

Table 1. Global quantitative properties of the flocks

Flocking event	Number of birds	Volume (m ³)	Density ρ (m ⁻³)	NND r ₁ (m)	Velocity (m/s)	Balance shift	Thickness I ₁ (m)	Aspect ratios		Orientation parameters			
								I ₂ /I ₁	I ₃ /I ₁	I ₁ ·G	V·G	V·I ₁	
32-06	781	930	0.80	0.68	9.6	0.03	0.08	5.33	2.97	4.02	0.89	0.06	0.20
28-10	1246	1840	0.54	0.73	11.1	0.34	-0.06	5.29	3.44	6.93	0.80	0.09	0.41
25-11	1168	2340	0.38	0.79	8.8	0.37	-0.10	8.31	1.90	5.46	0.92	0.12	0.14
25-10	834	2057	0.34	0.87	12.0	0.05	0.00	6.73	2.65	4.98	0.99	0.18	0.18
21-06	617	2407	0.24	1.00	11.2	0.04	0.00	7.23	2.56	4.53	0.96	0.09	0.11
29-03	448	2552	0.13	1.09	10.1	0.20	0.00	6.21	3.58	5.96	0.97	0.27	0.06
25-08	1360	12 646	0.09	1.25	11.9	0.19	0.16	11.92	3.32	5.12	0.95	0.14	0.12
17-06	534	5465	0.08	1.30	9.1	0.18	0.50	9.12	2.76	6.94	0.91	0.09	0.32
16-05	2631	28 128	0.06	1.31	15.2	0.15	0.00	17.14	2.46	8.36	0.90	0.19	0.25
31-01	1856	33 487	0.04	1.51	6.9	0.24	0.17	19.00	2.44	4.07	0.95	0.09	0.13

Flocking events are labelled according to session number (each day of data taking corresponding to a session) and position within the session (in temporal order). Each quantity was averaged over the different shots of the event. Events are ordered by increasing values of the average nearest-neighbour distance (NND), r_1 . The density was computed as the number of internal birds divided by the volume of the flock, as defined with the α -shape. Velocity refers to the centre of mass (the average position of all birds in the flock). Concavity is defined as the relative volume difference between the actual and the convex border of the flock. The balance shift is defined as the relative difference along the direction of motion between the position of the centre of mass and the geometric centre of the flock: positive values indicate that the density is larger on the front. The thickness I_1 , the two larger dimensions I_2 and I_3 , and the corresponding aspect ratios, are defined as described in the [Methods](#). The last three columns report the scalar products (absolute values) between yaw (the axis relative to the shortest dimension), gravity, \mathbf{G} , and velocity, \mathbf{V} .

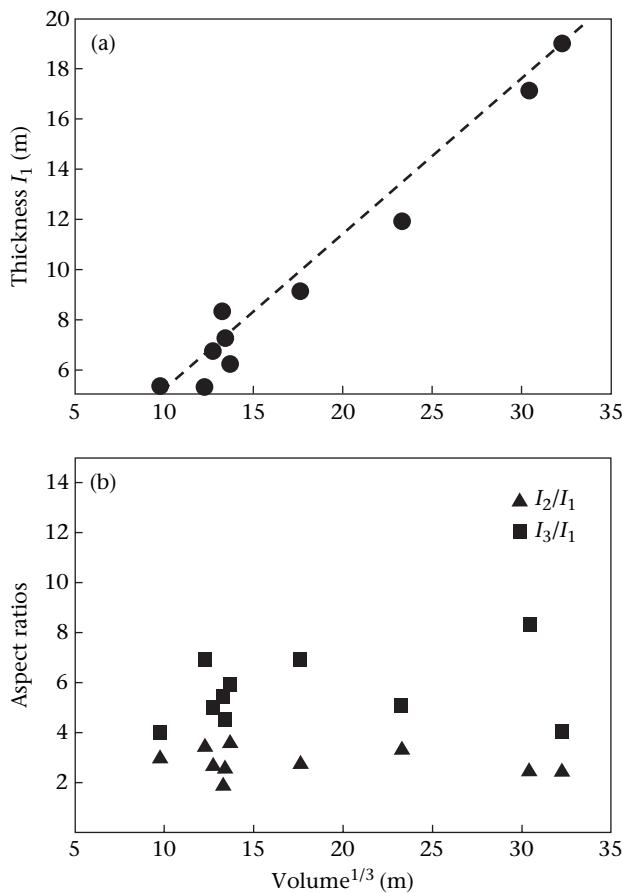


Figure 2. Dimensions and aspect ratios. (a) The flock's thickness I_1 is plotted against $V^{1/3}$, where V is the volume, for all the 10 events we analysed. The dashed line represents a linear fit of the data (Pearson correlation: $r_8 = 0.97$, $P = 1.6 \times 10^{-7}$). (b). Aspect ratios, i.e. the ratios of the two longer dimensions to the shortest dimension, I_2/I_1 and I_3/I_1 , in relation to volume (I_2/I_1 : $r_8 = 0.24$, $P = 0.51$; I_3/I_1 : $r_8 = 0.22$, $P = 0.54$).

for most events (Fig. 3). On average, $|\mathbf{V} \cdot \mathbf{G}| = 0.13 \pm 0.05$ and $|\mathbf{V} \cdot \mathbf{I}_1| = 0.19 \pm 0.08$. Velocity was thus approximately perpendicular to gravity and yaw. This result, together with the fact that yaw and gravity were nearly parallel to each other, implies that most of the time flocks moved horizontally, flying approximately parallel to the ground.

Finally, we can look at the orientation of the flock with respect to the other two axes, \mathbf{I}_2 and \mathbf{I}_3 . The scalar product of the velocity with each of these two vectors changed significantly from flock to flock, and, in some cases, it also changed across time. Some flocks appeared to be elongated in the direction of motion (i.e. the velocity direction), having a large value of $|\mathbf{V} \cdot \mathbf{I}_3|$, whereas for other flocks the opposite was true, with a large value of $|\mathbf{V} \cdot \mathbf{I}_2|$. We therefore, found no correlation between direction of motion and elongation of the aggregation.

Turns

An interesting problem is how birds coordinate their movements during turns. This requires analysis of events

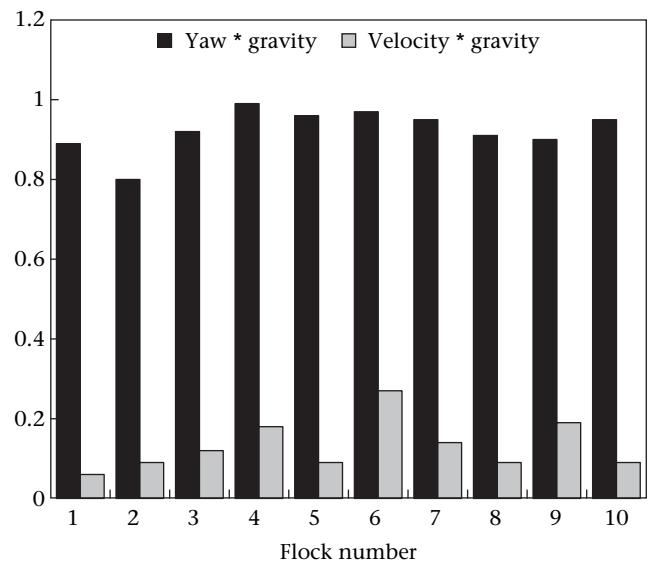


Figure 3. Orientation. The flock's orientation in space can be described by the mutual orientation of yaw (\mathbf{I}_1), velocity (\mathbf{V}) and gravity (\mathbf{G}). In most flocks, the inner product (in modulus) between yaw and gravity ($|\mathbf{I}_1 \cdot \mathbf{G}|$) was close to one but the inner product (in modulus) between velocity and gravity ($|\mathbf{V} \cdot \mathbf{G}|$) was small.

that are long enough to include a turn. Event 32-06 was almost 4 s long, it moved parallel to the ground (Fig. 4b) and the projection of its trajectory on the plane perpendicular to gravity (the horizontal plane) showed a clear turn (Fig. 4a). The unit vectors \mathbf{I}_2 and \mathbf{I}_3 associated with the dimensions I_2 and I_3 identify the two orthogonal axes of the flock on the horizontal plane. The aspect ratio of this flock on the plane remained approximately constant throughout the turn ($I_3/I_2 \sim 4/3$). The turn was accompanied by a rotation of the velocity \mathbf{V} with respect to \mathbf{I}_2 and \mathbf{I}_3 . This can be seen clearly from the time evolution of the angles between the projection of the velocity \mathbf{V} on the plane and the axes \mathbf{I}_2 and \mathbf{I}_3 : for example, the angle between the projection of \mathbf{V} and \mathbf{I}_3 was slightly larger than 90 degrees at the beginning of the curve, whereas it was 0 degrees at the end of the turn (Fig. 4c). Hence the flock's orientation changed with respect to the velocity, but it remained approximately constant with respect to an absolute reference frame (Fig. 4d). We found the same in three other flocks that displayed turns (events 17-06, 25-08, 28-10).

Another interesting behaviour can be observed in event 32-06. Before the turn the flock was in standard level flight, sliding horizontally. When the turn began, however, the flock tilted the yaw axis \mathbf{I}_1 with respect to the vertical, and thus the angle between \mathbf{I}_1 and \mathbf{G} increased (Fig. 4e). At the same time, \mathbf{I}_1 acquired a nonzero component in the direction of motion, and therefore the angle between \mathbf{I}_1 and \mathbf{V} decreased. These two results indicate that when the turn was initiated the yaw axis of the flock rolled (or banked) in the direction of the turn (velocity and gravity remained orthogonal to each other). As a consequence, during the turn the flock's plane did not slide parallel to the ground, but underwent a finite drag. This flock's manoeuvre is reminiscent of an aircraft's banking turn. However, the aircraft rotates in the direction of the turn (the front of

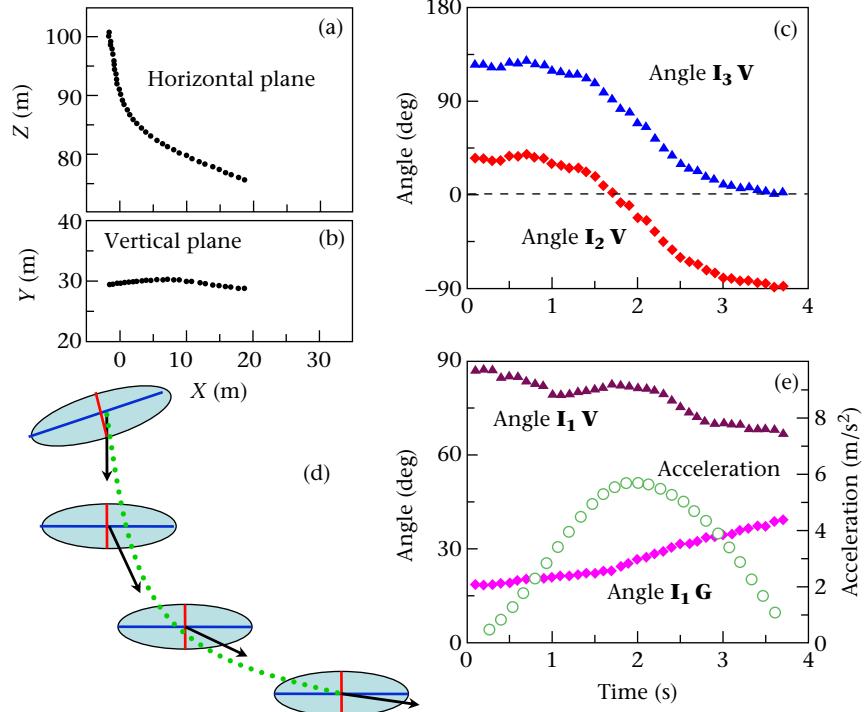


Figure 4. A turning flock. Event 32-06 lasted 4 s before the flock left the camera's field of view. (a) The trajectory of the flock projected on the horizontal plane (orthogonal to gravity) clearly shows a turn (direction of motion is left to right). Each point represents the (X, Z) position of the centre of mass of the flock, at time intervals of 0.1 s. (b) The same trajectory, when projected on the vertical plane (X, Y) (with Y parallel to gravity) looks very thin, showing that the flock flew parallel to the ground. (c) The angles between the planar orthogonal axes \mathbf{I}_2 and \mathbf{I}_3 of the flock and the projection of the velocity \mathbf{V} on the plane versus time. The velocity rotated with respect to \mathbf{I}_2 and \mathbf{I}_3 : at the beginning of the turn the velocity was approximately perpendicular to the longest axis \mathbf{I}_3 , whereas \mathbf{V} and \mathbf{I}_3 were parallel at the end of the turn. (d) Schematic representation of the flock's turn on the horizontal plane; \mathbf{I}_2 (red), \mathbf{I}_3 (blue) and \mathbf{V} (black) have mutual orientation as in the real event. Apart from a slight rotation early on, the absolute orientation of the flock remained constant throughout the turn. (e) The yaw axis \mathbf{I}_1 , orthogonal to the flock's plane, was almost parallel to gravity and perpendicular to velocity before the turn. As the turn approached, the angle between \mathbf{I}_1 and \mathbf{G} increased, whereas the angle between \mathbf{I}_1 and \mathbf{V} decreased. Hence, the yaw axis tilted in the direction of the turn, and the flock's plane was no longer parallel to the ground. The centripetal acceleration (in m/s^2) was computed from a Gaussian SP-line interpolation of the discrete trajectory. As expected, the acceleration showed a peak associated with the turn.

a plane always remains the same) and the mutual orientation of the velocity and the main aircraft axes (\mathbf{I}_2 and \mathbf{I}_3) does not change. In the case of a flock, as we have seen, the velocity rotates with respect to the main axes (what was the front becomes the side and vice versa). Moreover, there is no global lift on the flock, as it is not a unique rigid body. Therefore, even though individual birds will bank during the turn, it is unclear why the flock as a whole also does so, rather than simply sliding. A possible explanation is that it allows birds to keep their neighbours on the same visual plane, preserving visual information on their neighbours' positions.

Average Density and Nearest-neighbour Distance

One of our first questions concerned the density or the degree of compactness of the aggregations. We estimated the density ρ as the number of internal birds divided by the volume of the flock, as defined with the α -shape (see Methods). The values obtained for the 10 flocking events we analysed (Table 1) show that density varied

substantially across flocks. It did not depend on the number of birds belonging to the flock (Pearson correlation: number: $r_8 = 0.3$, $P = 0.39$; velocity: $r_8 = 0.47$, $P = 0.17$). An alternative measure of compactness, or rather of sparseness, is given by the average nearest-neighbour distance r_1 . This was sharply related to the density, ρ being proportional to r_1^{-3} , as expected for a homogeneous arrangement of points (Stoyan & Stoyan 1994; Fig. 5a). The nearest-neighbour distance r_1 also did not depend on the size of the group, contrary to the pattern observed in fish schools (Partridge et al. 1980) and computer simulations, (Kunz & Hemelrijk 2003). The values of r_1 show once again that the flocks we analysed were heterogeneous: nearest-neighbour distance varied more than 100% between the densest and sparsest events (Fig. 5b).

Density Variations Within the Aggregation

A further important question concerns density variations through the group: is there any significant density gradient in the flock? To answer this question we investigated how density or, alternatively, sparseness, changed as one moved from the border to the centre of the flock. We divided the

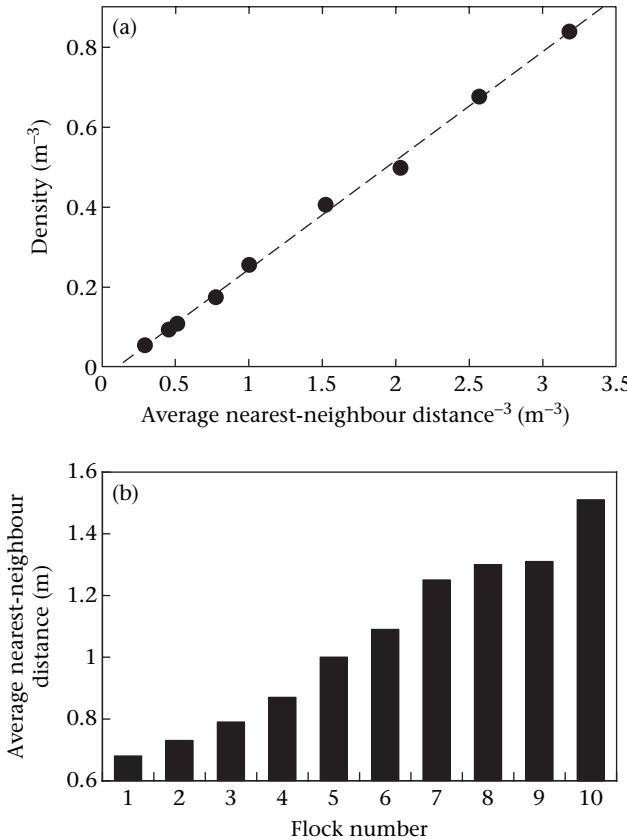


Figure 5. Nearest-neighbour average distance. (a) The density ρ of the flock in relation to the average nearest-neighbour distance r_1 ($\rho \propto r_1^{-3}$; Pearson correlation: $r_8 = 0.8$, $P = 0.0004$). We thus used r_1 as a convenient measure of a flock's sparseness. (b) The sparseness r_1 varied from 0.7 to 1.5 m in the analysed events. Average body length BL and wing span WS of starlings are, respectively, BL = 0.2 m and WS = 0.4 m (Feare 1984), and thus in the densest flocks $r_1 \sim 3.5BL$ and $r_1 \sim 1.7WS$.

flock into shells of thickness δ , moving from the border to the centre. One shell was defined as the subset of birds that are found at a distance $d < k\delta$ from the border, with $k = 1, 2, 3, \dots$. Within each shell, we measured the average nearest-neighbour distance. In this way, we obtained the nearest-neighbour distance r_1 as a function of the distance from the border, d . The behaviour of $r_1(d)$ for our flocks was radically different from that of a homogeneous system (Fig. 6a). The nearest-neighbour distance increased from the border to the centre: flocks had a higher density close to the border (small r_1) and were more sparse in the centre (large r_1). We also looked directly at a density measure by defining a gradient function from the border to the centre. For a given value of δ , we erased all the birds with $d < \delta$, that is, the birds close to the original border. We were then left with a reduced set of birds where the outer shell had disappeared. We computed the border of this new set using the α -shape method, its volume and, finally, its density. We iteratively recomputed the density until we reached the core of the flock. For $\delta = 0$ this basically corresponds to peeling away layers of the flock progressively. This measure shows that density was higher close to the border

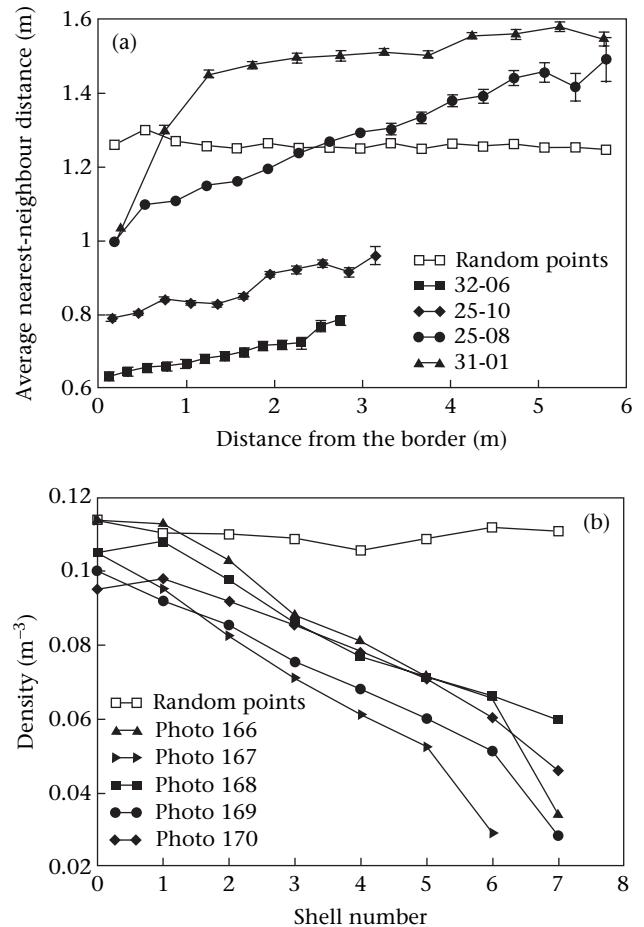


Figure 6. Density gradient. (a) Average nearest-neighbour distance as a function of the distance from the border, for four flocking events. Each curve was obtained by averaging over the consecutive shots of the corresponding event (error bars indicate SEs arising from the corresponding fluctuations). In all the flocks the average nearest-neighbour distance increased from the border to the centre, indicating that flocks were denser at the border. We also report the behaviour of a Poisson ensemble of random points of density and dimensions comparable to event 25-08: for a homogeneous system the average nearest-neighbour distance is constant and does not depend on the distance from the border. (b) Density as a function of the shell number. To compute the density, the birds in a shell of length $\delta = 0.2$ from the border were erased, then the border of the reduced set of birds was recomputed, and finally its density obtained as the ratio of the number of internal birds to the reduced volume. The procedure was repeated until no birds were left in the reduced set. The curves correspond to single consecutive shots in event 25-08, where the density gradient is more evident and the number of birds is large enough for single-sample statistics. To compare with the random homogeneous case, and to be sure that small volume effects do not bias the decrease in density, we generated a set of random points with the same border, volume and internal density as photo 166 of flock 25-08. In the other events the density gradient is qualitatively similar.

(Fig. 6b). This density gradient was larger in some flocks than in others but was qualitatively present in all 10 flocks we analysed.

To investigate whether there was also a front to back density imbalance, we computed the balance shift, defined as the relative difference along the direction of motion

between the position of the centre of mass and the geometric centre of the flock. Positive values of the balance shift mean that the centre of mass is located more towards the front of the flock with respect to the geometric centre, and that there is therefore a net imbalance of birds in the front. Table 1 gives the values of the balance shift for all the analysed events. Sometimes the birds were concentrated more towards the front of the flock (four flocks), sometimes more towards the back (two flocks), and sometimes they were uniformly distributed in the outer shell.

Nearest-neighbour Radial Distribution and Exclusion Zone

To gain an insight into the interindividual structure of the flock, we looked at the probability distribution of the nearest-neighbour distance, $P(r)$ (Fig. 7). The shape of this function is reminiscent of that of a random (Poisson) set of points. There are, however, important differences. Most notably we observed that $P(r)$ dropped at low values of r and, correspondingly, that the cumulative probability $P^>(r)$ was shifted compared to the Poisson case. The biological origin of this drop is rather intuitive: birds maintained a certain distance from each other, to avoid collisions. For this reason, most numerical models for collective behaviour assume the existence of short-distance repulsion, which

gives rise to an ‘exclusion zone’ around each individual. This is equivalent to hard-core repulsion in particle systems. To measure the exclusion zone, we fitted the probability distribution of nearest-neighbour distance to that of a hard-core system (Torquato 2002). We found that the size of the exclusion zone was very stable across flocks and did not correlate with sparseness r_1 (Pearson correlation: $r_8 = 0.21$, $P = 0.56$). The average \pm SE over all flocks gives $r_h = 0.19 \pm 0.02$ m. Therefore, the average minimum bird-to-bird distance ($2r_h \sim 0.38$) was larger than a starling’s typical body length (0.2 m), but was comparable to the typical wing span (0.4 m; Feare 1984).

Nearest-neighbour Angular Distribution

Finally, we considered the angular distribution of the nearest neighbours. To do this, for each individual bird, we considered the vector to its nearest neighbour and measured the angle θ between this vector and the direction of motion of the flock. The distribution of $\cos(\theta)$ should be constant and equal to 0.5 for an isotropic system. For example, for a completely random arrangement of birds the neighbours can be found anywhere around the focal one. The probability of finding a neighbour at angle θ can be computed by assuming a constant bird density in space. If we choose the direction of motion as the polar axis, then this probability is simply given by $P_{\text{random}}(\theta)d\theta = 1/2 \sin(\theta)d\theta$, where the

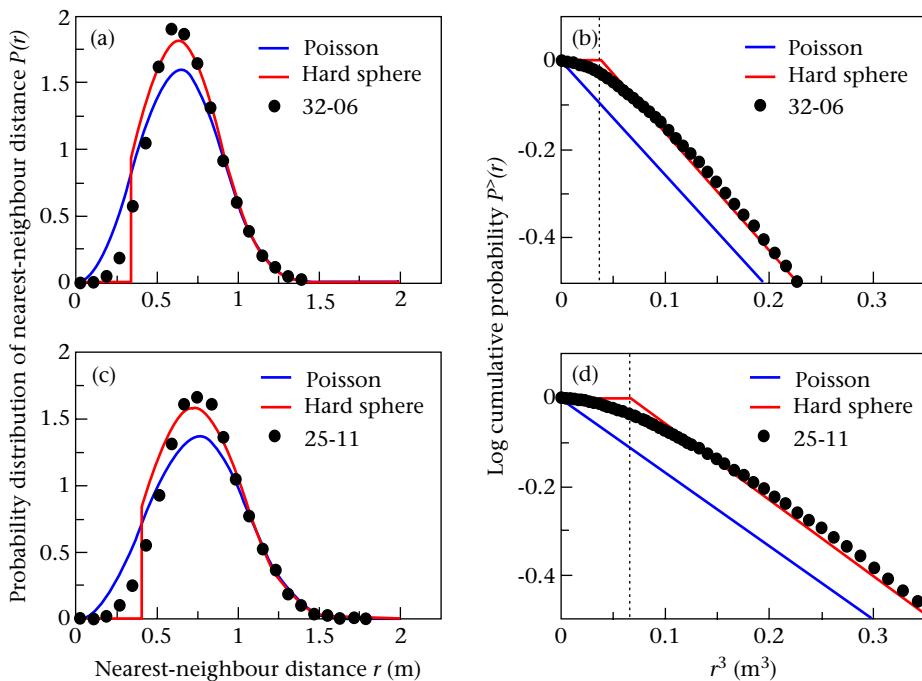


Figure 7. Nearest-neighbour distance distribution and hard core. (a) Event 32-06: probability distribution $P(r)$ of the nearest-neighbour distance. The average nearest-neighbour distance r_1 is the average of r with this distribution. Compared to a Poisson fit, the data showed a drop in probability at small values of r . Birds (on average) tended not to get closer than a certain minimum distance. In this sense, we say that birds have an effective hard core r_h . As a consequence, the nearest-neighbour probability distribution of a hard-sphere system, which is zero for $r < 2r_h$, is a better fit of the data. (b) The presence of a hard core is particularly evident when one plots the logarithm of the cumulative probability $P^>(r)$ (the probability that the nearest-neighbour distance is larger than r) as a function of r^3 . The hard-sphere cumulative probability is equal to 1 for $r < 2r_h$, where r_h is the hard core. Thus, compared to a Poisson fit, the hard-sphere curve has a shift caused by the presence of the hard core. This shift is clearly present in the real data. For event 32-06 the hard-sphere fit gives $r_h = 0.17$ m (the value of $2r_h$ is marked by the vertical dotted line). (c, d) Event 25-11, same symbols as in (a, b). Hard core $r_h = 0.20$ m.

factor $\sin(\theta)$ is the Jacobian from Cartesian to polar coordinates. Thus, even in a random isotropic system the distribution of θ is not constant. On the other hand, a simple change of variables gives $P_{\text{random}}(\cos(\theta))d\cos(\theta) = 1/2$, and the distribution of $\cos(\theta)$ is therefore constant for a random isotropic system (see Cavagna et al. 2008b for more details). It is therefore much more convenient to look at this distribution to distinguish anisotropic from isotropic arrangements of neighbours. We plotted the distribution of $\cos(\theta)$ for four flocks (Fig. 8). In some flocks the distribution peaked at $\cos(\theta) = 0$ indicating that the nearest neighbour was more likely to be found on the plane perpendicular to the velocity (as in the flocks corresponding to Fig. 8c, d); in other cases (Fig. 8a, b) there were two well-defined peaks at intermediate angles indicating a more structured distribution in space. However, for all the analysed flocks, there was a lack of neighbours along the direction of motion ($P(\cos(\theta)) \ll 0.5$ for $\cos(\theta) \sim \pm 1$).

DISCUSSION

Our study is the first large-scale study of collective animal behaviour in a biological system. Some of our results (e.g. the exclusion zone or the density range) can be used as input parameters of existing models. Most of the results, however, should be used to refine and extend the models, to verify and assess their assumptions, and to identify the most appropriate theoretical framework. In addition, our results obviously have relevance for several general biological issues.

Morphology

Perhaps the most interesting morphological result is that flocks seemed to have a characteristic shape, being thin in the direction of gravity and more extended perpendicular to it. The proportions of the flock were well defined, with only weakly fluctuating aspect ratios, despite showing a wide range of sizes (Table 1). Our ability to conclude this stems entirely from the fact that we were able to analyse several groups with very different sizes (dimensions and number of birds). Nonspherical shapes have also been observed in fish schools, the average proportions $I_1:I_2:I_3$ ranging from 1.0:1.7:2.1 in pilchards, *Harengula humeralis* (Cullen et al. 1965) to 1.0:3.0:6.0 in saithes, *Pollachius virens*, and 1:3:4 in herrings, *Clupea harengus* (Partridge et al. 1983). These values are comparable to those we found for starlings: 1.0:2.8:5.6. These studies, however, were limited in two respects: first, group size was a few tens of individuals, so the researchers could not check whether the proportions remained stable at different sizes; second, it is unclear to what extent the shape of the tank and the water depth influenced the group's morphology.

In our analysis, using a much larger statistical sample, we verified that, while the smallest dimension was strongly correlated with volume and number of individuals, the flock was organized in a way that maintained its proportions. This raises a number of interesting questions. Do these proportions serve any function? Is it the individuals themselves or some external stimulus that keeps the group's

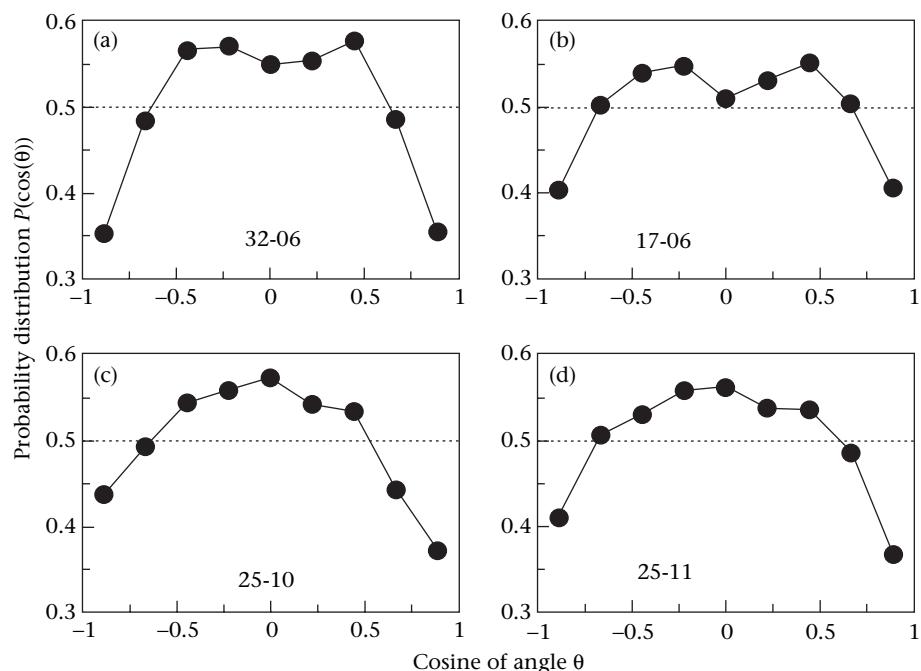


Figure 8. Nearest-neighbour angular distribution. (a–d) Probability distribution of the cosine of the angle θ , that is, the angle between the global flock's velocity and the direction of the nearest neighbour, for events 32-06, 17-06, 25-10 and 25-11. $\cos(\theta) = +1$ corresponds to the front of the reference bird, whereas $\cos(\theta) = -1$ corresponds to the back. For an isotropic arrangement of points there is no correlation between velocity and position of the nearest neighbour; therefore all directions are equally probable, and this probability distribution is constant and equal to 1/2 (provided that boundary effects are appropriately accounted for). The isotropic value 1/2 is marked as a dotted line in the figure. All 10 flocks we analysed showed a significant drop in probability at $\cos(\theta) = \pm 1$, indicating that the arrangement was not isotropic and that the nearest neighbour of each bird was less likely to be found around the direction of motion.

proportions constant? If the individual birds are responsible, how do they achieve this, starting from a purely local perception of the aggregation?

There may be a general reason why some specific proportions have been selected. For fish schools a thin shape may minimize the chance of being seen by distant predators (Partridge et al. 1983). Alternatively, one could argue that this thin elongated shape is a direct consequence of the mechanisms leading to group formation and does not have any adaptive function. Numerical simulations of fish schools (Kunz & Hemelrijk 2003; Hemelrijk & Hildenbrandt 2008) show that aggregations produced with simple local interactions acquire an elongated shape in the direction of the velocity. This correlation between elongation and velocity was suggested long ago on purely biological principles (Breder 1959; Radakov 1973) and was later observed in fish schools (Pitcher 1980). We did not, however, find any evidence of a similar pattern: the aspect ratios did not depend significantly on the absolute value of the velocity and there was no correlation between the longest axis and the velocity direction. This suggests that this feature may differ between birds and fish and that, in the case of bird flocks, the global shape of the groups may not be fully explained by the interactions between individuals.

The morphology of the flocks may also be influenced by the aggregation dynamics between groups. Recent models of aggregation–fragmentation (Okubo 1986; Bonabeau et al. 1999) have been used successfully to predict scaling in the size distribution of several species (from fish school to herds of ungulates). These models may be helpful to investigate the origin of the shape of the groups. The rules of fission and fusion between groups, however, need to be generalized to this purpose. They were assumed to be isotropic in the past, but this may not be the case in reality. For example, studies on fish schools have shown that they become multilayered as the number of individuals increases (Partridge et al. 1980).

Gravity may also explain the thin shape that we observed: up/down space fluctuations are energetically more costly than lateral ones, favouring the stretching of the aggregation along the plane perpendicular to gravity. Finally, from an aerodynamic point of view, a simple model shows that there is a net decrease in drag when the flock extends further laterally than vertically (Higdon & Corrsin 1978).

Orientation

All the flocks we analysed had a well-defined orientation in space: velocity and gravity were approximately perpendicular, whereas yaw and gravity were nearly parallel. In other words, the flocks moved horizontally, flying almost parallel to the ground. This may seem odd to anyone who has observed flocks. The reason for this is that we typically watch from the ground, with our heads tilted up, so we are unable to distinguish between closer and more distant birds. As a result, we project the flock onto our tilted plane of vision, thus losing perception of its orientation and relatively thin aspect. It is possible, however, that the flight orientation is different in more dramatic events than the

ones we considered (as in the case of a predator's attack or for flocks at higher altitudes).

When looking for possible explanations of this behaviour, it is reasonable to expect gravity to be important for the flock's relative orientation. Migratory flocks and flocks travelling from feeding to roosting sites show level flight parallel to the ground, and typically spread out horizontally rather than vertically (Major & Dill 1978). Several kinds of fish also form almost two-dimensional schools that swim parallel to the water's surface (Cullen et al. 1965; Partridge et al. 1983). Gravity directly determines individual kinematics which occurs at a lower cost orthogonal to gravity: starlings perform steady level flight or intermittent undulating flight (temporarily gaining or losing altitude during flapping and gliding periods) where, in any case, the optimal flight strategy corresponds to a mean flight path that is level (Rayner et al. 2001). In other words, birds tend to fly, on average, parallel to the ground because of energetic considerations.

Turns

We observed that, during a turn, the flock's orientation changed with respect to velocity: if the flock was originally moving in the same direction as the intermediate axis, at the end of the turn it ended up oriented along the longest axis (Fig. 4c). This explains why we did not find any statistically preferred orientation of flocks with respect to the direction of motion: flocks remained over the roost and turned continuously, so that their relative orientation with respect to velocity changed continuously.

Pomeroy & Heppner (1992) described the mechanism of turning in a group of 12 rock doves, *Columba livia*, and showed that birds turn in equal-radius paths, rather than parallel paths. For example, in a 90-degrees left-turn, birds at the front of the flock end up on the right of it, whereas those on the left of the flock end up at the front of it (Fig. 4d). In this way what was the front-to-back axis before the turn becomes the side-to-side axis after the turn. The mechanism described by Pomeroy & Heppner is confirmed by our empirical observations here: if birds turn along equal-radius paths, it follows that, as we have shown, the velocity must rotate with respect to the flock's planar axes. Note that, unlike equal-radius paths, parallel paths would require very different accelerations of the individuals during the turn, to retain the shape of the flock, which is what we observed. Consideration of energetic would suggest this is unlikely to occur.

This turning mechanism leads to several interesting issues. From the point of view of the individual, group membership is advantageous for its antipredator benefits. However, not all the positions in the aggregation are equivalent, and, under some circumstances, some positions may be more advantageous than others. For example, birds at the boundary of the flock typically suffer a higher predation risk. If the cost/benefit balance were negative for too many individuals or for too long, the group would eventually break up. Given that, in general, animal aggregations are rather stable, this implies that group structure and dynamics must allow for a systematic redistribution of risk among their members.

Individuals must be able to move through the flock and exchange positions, while at the same time maintaining the integrity of the group. We found that the front, sides and back of the border were not stable regions of the flock. Rather, they continuously switched. This indicates that there were no long-lasting privileged positions along the border, so that the risk/benefit of any boundary location is periodically readjusted. It would be interesting to know whether there is an analogous turnover with respect to the border–centre direction. Future work on individual trajectories will allow us to answer this question.

Average Density and Nearest-neighbour Distance

Our results on the internal structure of the groups showed that the density and the average nearest-neighbour distance of the flocks did not depend on the size of the group. This is contrary to observations of fish schools (Partridge et al. 1980) and the results of theoretical models (Kunz & Hemelrijk 2003; Hemelrijk & Hildenbrandt 2008), where the average nearest-neighbour distance was found to increase as the number of fish in the group increased. However, in both of these studies, the average nearest-neighbour distance was computed without taking into account the bias introduced by the border and, consequently, they do not give an accurate measure of group density. Individuals located on the border had a nearest-neighbour distance that was larger than that typical of internal individuals, simply because part of their surrounding volume was empty (see Cavagna et al. 2008b for a more detailed discussion of border effects). Given that the percentage of individuals on the border decreases, as groups get larger, ignoring border effects means that the average nearest-neighbour distance will inevitably decrease with group size, even if the density of groups remains the same at all sizes.

Another interesting result, shown clearly in Table 1 and Fig. 5b, is that density varied considerably across flocks and there was not a well-defined typical value. Of course, this may be caused by the limited number of flocks we analysed (10) and a larger sample could reveal a distribution of densities that peaks at a characteristic value. Even if this were so, however, it remains true that density fluctuations across flocks were very large. In addition, density did not depend on the size of the flock (contrary to observations of small fish schools, Partridge 1980). This leaves open the question as to what exactly determines the density of a flock. Clearly, there are some relevant biological factors to consider, such as the presence of predators (falcons) or disturbance (e.g. by seagulls). When under attack, a flock shows fast expansions and contractions, indicating that strong perturbations have a direct effect on density. This cannot explain the variation we see here because the events we analysed did not involve predator attacks.

Many models of self-organized motion assume that the interaction between individuals depends on their mutual distance in space. In such cases, the average interindividual distance (and therefore density) is determined by the specific relation between interaction and distance. An individual is attracted to its neighbours at large distance,

to remain part of the flock; at short distances, however, it is repelled, to avoid collisions. For a given distance, the attraction and repulsion forces will compensate for each other and the net force experienced by the individual will be null: this value becomes the average nearest-neighbour distance of the model. In a recent work, however (Ballerini et al. 2008), we have shown by analysing 3D data that interactions between individual starlings do not depend on their metric distance in space, but rather on their topological distance (i.e. whether they are first, second, third ... neighbours). This means that there cannot be a well-defined distance in space where the force felt by one bird is null and therefore the global density is not simply related to microscopic interactions.

Density Variations Within the Aggregation

All flocks had a density gradient: density was higher at the border than in the centre. This result is surprising, given that some models of collective animal behaviour predict exactly the opposite (e.g. Kunz & Hemelrijk 2003). The explanation for this is possibly to be found in the antipredator response of the aggregations.

The evolutionary motivation for grouping has been associated traditionally with its antipredator function (Vine 1971; Parrish 1992; Pitcher & Parrish 1993). Belonging to a group of similar individuals decreases the probability of being caught (dilution effect). Moreover, moving together also reduces the ability of a predator to focus on a specific individual and capture it. The response to predators is likely to optimize this confusion effect, as can be seen in the very effective escape manoeuvres of starling flocks under attack. The high-density borders that we observed may represent a feature that enhances such antipredator tactics, creating a ‘wall’ effect to increase the predator’s confusion. However, we do not at present understand how the density gradient is produced in terms of interindividual dynamics within the group. Reconstruction of the individual dynamic trajectories, which is currently underway, will help to clarify this point.

Finally, some numerical models of fish schools reveal that density is higher at the front of the group (Kunz & Hemelrijk 2003; Hemelrijk & Kunz 2005; Hemelrijk & Hildenbrandt 2008), as also observed in natural shoals (Bumann et al. 1997). In our analysis, however, we did not find a clear and general correlation between the densest part of the flock and the direction of motion.

Nearest-neighbour Radial Distribution and Exclusion Zone

An important result concerned the presence of a well-defined exclusion zone around individual birds, which was very stable across flocks and whose diameter was comparable to the average wing span. The finding that birds did not come too close to one another is highly intuitive, given the need to avoid collisions, and is consistent with one of the main assumptions of numerical models. Models for flocking that use the size of the exclusion zone as an input parameter can now be fed with our empirical value to increase their accuracy.

We stress that the value of the exclusion zone (ca. 0.38 m) does not depend on density, and that it provides a metric scale characteristic of flocking behaviour. As already mentioned, a second study on the same data set (Ballerini et al. 2008) shows that the interaction between birds has a crucial topological character: each individual interacts with up to six or seven neighbours, irrespective of their distance. It seems, therefore, that the interaction between birds can be understood at two levels: metric at short scales and topological at larger ones. In other words, when a neighbour is too close, a bird takes into account its physical distance and tries to keep it outside the exclusion zone; for more distant birds, however, the actual distances do not matter and the bird interacts up to its seventh neighbour, wherever it is located in space. The reasons for such behaviour are inherent in the very nature of flocking and aerial display. On the one hand, individuals in a group must avoid collisions and control the mutual dynamics at short distances. On the other hand, the flock undergoes large density variations that can modify dramatically the distances of nearest neighbours: to keep the same degree of cohesion, indispensable during predator attacks, each bird must keep track of the same number of neighbours, even if their distances change.

The analysis of nearest-neighbour distributions using a hard-sphere model also revealed another quantitatively important feature: flocks were not as compact as they may appear to an observer. For hard spheres, the degree of compactness of the system can be classified through the so-called packing fraction: $\phi = 4/3\pi\rho r_h^3 = vN/V$, where ρ is the density, r_h the size of the hard core (the exclusion zone), v is the volume of each sphere, N is the total number of spheres, and V is the volume of the aggregation. The packing fraction is simply the ratio between the total volume occupied by the spheres and the volume of the aggregation. It depends only on the hard-core value and on the density and, by definition, it is a number between 0 and 1. Small values of ϕ correspond to very diluted systems (gas-like) and large values correspond to compact ones (liquid or crystals). To give some quantitative reference values: compact crystalline arrangements of spheres correspond to $\phi > 0.490$ and the value for the most compact possible arrangement is $\phi \sim 0.79$ (the so-called random close packing, Torquato 2002). All the flocks we analysed showed packing fractions smaller than 0.012. This is a very small value indeed. In hard-sphere language, flocks are thus extremely sparse systems, with much lower densities than a crystalline arrangement. This sparseness is not evident to the eye, since the two-dimensional projection we perceive looks much denser. This sparseness makes good biological sense because, if the birds were too close to each other, exchange of positions and diffusion inside the flock would be difficult to achieve. Further analysis on individual birds' trajectories will allow us to investigate more quantitatively the extent to which the individual freedom to move is related to the overall flock density.

Despite being such sparse systems, flocks had a nontrivial structure in space, which was well described by the angular distribution of nearest neighbours. Neighbours were less likely to be found along the direction of motion; instead, they concentrated laterally. Although the comparison with particle systems can be extremely useful from

a methodological point of view, one always has to keep in mind that animal groups are very different. A hard-sphere system with the same hard-core and density values as those we found here would be a gas without any structure, whereas the flocks had a strongly anisotropic structure. Reproducing such features will be an ongoing challenge for models and theories.

Nearest-neighbour Angular Distribution

A similar spatial anisotropy to the one we found for starlings has been reported in fish schools (Partridge et al. 1980), suggesting this is a typical feature of collective behaviour in both birds and fish. An important question, therefore, is to understand the origin of this anisotropy. One possibility is that it is simply an effect of the existence of a preferential direction of motion. However, the simplest numerical models of self-organized motion, which assume isotropic interactions between individuals, give a nonzero velocity for the aggregation, but fail to reproduce the angular anisotropy. This suggests that the anisotropy in the nearest-neighbour distribution is an explicit consequence of the anisotropic character of the interaction itself, which modellers should incorporate into their assumptions if they want to reproduce the observed behaviour.

There are various reasons why interactions between individuals should be anisotropic. First, we note that vision itself has an anisotropic nature in both birds and fish. In particular, starlings have lateral visual axes and a blind rear sector (Martin 1986). Thus, if vision is the main mechanism by which interactions are controlled, then the very structure of the eye may be responsible for the lack of nearest neighbours in the front–rear direction (Heppner 1974; Badgerow 1988; Speakman & Banks 1998). An alternative idea is that the mutual position chosen by the animals is the one that maximizes the sensitivity to changes of heading and speed of their neighbours (Dill et al. 1997). According to this hypothesis, even though the interaction is still vision based, it is an optimization mechanism to determine the anisotropy of neighbours. Another possibility is that individuals try to keep more distance between themselves and the individuals in front of them, to avoid the risk of collisions in case of sudden changes of velocities.

Finally, a radically different claim is that anisotropic structures in both bird and fish aggregations save energy thanks to aerodynamic (or hydrodynamic) advantages (Lissaman & Shollenberger 1970; Weihs 1973; Hummel 1995). The energy-saving principle has been challenged, however, for both birds (Badgerow & Hainsworth 1981) and fish (Partridge & Pitcher 1979). More importantly, at least for aerial display, the fact that interindividual interactions depend on the order of the neighbour rather than on their distance rules out aerodynamic arguments, because these imply a strong dependence on the metric distance (as discussed in Ballerini et al. 2008).

Conclusions

In this paper we have presented large-scale data on starling flocks during aerial display. Our data were

obtained in field observations of large, naturally occurring groups. This is, we believe, a very important feature, which distinguishes our study from previous ones. Experiments in the laboratory may condition some important features of the groups, such as their shape and dynamics, owing to the confined space. Groups of small size, both in the laboratory and in the field, do not allow a reliable statistical analysis because of border effects. Thanks to our experimental procedure, we avoided these two problems and produced, for the first time, unbiased data on very large groups in the field.

We investigated the main features of the flocks (shape, movement, density and structure) and characterized them as emergent attributes of the grouping phenomenon. Our data provide a new experimental benchmark for testing and improving theoretical models of self-organized motion. In this light, we discussed some of our results in connection with the known predictions of existing models. We hope that our analysis will help to clarify the fundamental microscopic mechanisms leading to collective behaviour in animal groups, and how appropriate behavioural rules for the individuals can determine specific features of the aggregation at the group level.

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